jurnal 11 vol100

by Universitas Simalungun (USI)

Submission date: 13-Aug-2022 12:57AM (UTC-0500) Submission ID: 1881990858 File name: 11Vol100No12-Jurnal_Q4_1_1.docx (387.74K) Word count: 5428 Character count: 24659 © 2022 Little Lion Scientific

ISSN: 1992-8645

www.jatit.org



NEIGHBORHOOD SEARCH METHOD

MARLAN¹, HERMAN MAWENGKANG²

¹Universitas Simalungun, Pematang Siantar, Indonesia

²Department of Mathematics, Universitas Sumatera Utara, Medan, Indonesia

E-mail: ²hmawengkang@yahoo.com

ABSTRACT

For a Periodic Vehicle Routing Problem (PVRP), this study offers a new mathematical model which optimizing vehicle travel expenses based on many assumptions. Periodic planning includes consideration of the following four issues that is a vehicle routing problem with time windows (VRPTW), a capacitated vehicle routing problem (CVRP), a vehicle routing problem with split service (VRPSS) and a vehicle routing problem with simultaneous pickup and delivery (VRPSPD). In large-scale issues, the computational complexity of this problem can be handled by any optimization program in a reasonable amount of time since it is based on a single model that we have created. In this paper a neighborhood search meta-heuristic is proposed.

Keywords: Periodic VRP, Logistics, Split Service, Meta-heuristic, Neighborhood Search

1. INTRODUCTION

The vehicle routing problem (VRP) is a general issue for specifying homogenous sets of routes and vehicles, wherein every vehicle begins at a garage and travels alongside a path to service a number of clients with identified geographic positions, and returns back to the garage when tour ends. The service might be anything from delivering things to picking up items to name a few. An essential part of the VRP is the depot, which stores and employed the vehicles to transport items to and from the depot, and the clients who receives the items. Reducing the overall transport route price while adhering to thorough going working time and vehicle capability limits is a fundamental goal of a VRP [1]. In spite of this, there may be various gaps among the fundamental VRP, and real-life implementation, for instance, depots quantity, client needs numerous pickups and deliveries, vehicles type with varied travel durations, capacity and expanses of travel, path restrictions and time frames of vehicles and so on. Variations, formulations, and solution procedures of VRPs were all examined indepth by [2]–[4].

In VRPs, Capacitated vehicle routing problem (CVRP) is the most often studied. Looking at a route's overall demand and VRP with time windows(VRPTW) in order to make sure that the

vehicle can handle it all [5] and [6]. [7] developed Open Vehicle Routing Problem (OVRP) with a novel mathematical model. The model utilizes reasonable time windows by means of which distributors want to serve clients sooner than competitors to maximize sales. They developed a multi-objective particle swarm optimization (MOPSO) approach as well as a widely used multiobjective evolutionary method (NSGA-II) was used to compare their outcomes. Extending vehicle routing models has also been attempted(for example several pickups and delivery positions VRP [8]–[10]. In addition, there is VRP with Simultaneous Pickup and Delivery (VRPSPD) wherein clients want both delivery and collection of items at the same time. There is a complete dynamic VRP model in [11], [12]. In the classical VRP, only one vehicle may service each node. Alternatively, more than one vehicle may service the client by numerous vehicles that pass through from that node. It is recognized as the VRP with the same split service (VRPSS) means that a service may be distributed across numerous vehicles [13].

Using VRP, one may come up with a schedule of services that is as cheap as possible [14]. A variation of VRP that develops routes is called PVRP. It was initially proposed as the Assignment Routing Problem in 1979, a mathematical model version of the Periodic Vehicle

30th June 2022, Vol.100, No 12

www.jatit.org

© 2022 Little Lion Scientific



ISSN: 1992-8645 www Routing Problem (PVRP) [15]. Minimum numbers of visits are established as every day nodes are not visited. After that, research was refined to take into consideration number of days that individual node had been visited [16]. As a result of this, PVRP

visited. After that, research was refined to take into consideration number of days that individual node had been visited [16]. As a result of this, PVRP research developed exponentially. Numerous sorts of items have been studied using PVRP in the past. It demonstrates that these issues really occur on a daily basis. In PVRP study, a variety of materials were utilized as an insight such as distribution of vegetables [17], auto parts [18], collecting garbage [15], [19] ,beverage distribution [20], utility services [21], home health care (HCC) logistics [22], and many others. The majority of PVRP research has been focused on developing heuristic approaches for solving problems. Using the heuristic technique, you can come up with an acceptable solution to your issue, but you can't be certain that you'll obtain the best one [23]. Heuristics method may be useful when the number of customers serviced is enormous. Several researchers have been looking for a PVRP heuristic solution, like using variable neighborhood search [24], neighborhood search [25], particle swarm [26], hybrid genetic algorithm [27], hybridization of tabu search [22], hybrid metaheuristic algorithm [28], and large adaptive neighborhood [29]. Numerous advancements have been made in PVRP research. In terms of PVRP, there are three primary groups: multi-depot PVRP (MDPVRP), PVRP with time windows (PVRPTW), and PVRP with service choice (PVRP-SC) [30]. [21], [31]demonstrate the presence of multi-depot PVRP. [24], [25], [31]-[34] explain PVRP using time windows. PVRP-SC, on the other hand, refers to PVRP that allows number of visits to be used as judgment variable in discovering solutions, as in study [35]. It is claimed that PVRP-SC exhibits properties similar to those seen in the Inventory Routing Problem (IRP). PVRP-SC and IRP's closeness to one another determines the visits frequency, arrangement of route, and deliveries in total[30]. The node's schedule determines the PVRPSC attributes combination and the quantity of items sent to the node. Among the features of the IRP issue is quantity of deliveries at node is a decision variable varies from the number of visits [35]. FPVRP was used to develop this issue [35] by adding its flexible qualities to it [32]. The term "flexibility" refers to the ability to alter the frequency and number of visits. Flexibility was factored by [32] which gave a fresh viewpoint on modeling. Heuristic technique by [36] was one research that looked at flexibility. An FPVRP algorithm solution was found by [32] in two phases. Initial solutions were developed in the

first phase, which was then followed by a tabu search process [37]. Additional advances in the two-tiered distribution channel with a flexible service time frame have been made [38]. Taking into consideration the consumer's discount, a model was also designed which allows for more flexibility in delivery time [39].

The structure of the research article is maintained as follows. First, an overview of the topic and a review of relevant literature are the first items on the agenda. Section 2 defines the mathematical model, and Section 3 presents the suggested approach based on neighborhood search for resolving the presented issue. In section 4, calculations and results are presented. Lastly, Section 5 sums up the findings of this article and recommends prospective research avenues for further investigation.

2. MODEL FORMULATIONS

Following are some examples of how this model might be described. Let G = (V, A) be a chart where $V = \{v_0, v_1, ..., v_n\}$ and A = $\{(v_i, v_i) | v_i, v_i \in V, i \neq j\}$ area set of arcs and a set of nodes, in that order. A has two matrices, one for the expense of travel (c_{ii}) and one for the time it takes to get there (t_{ij}) . Vertex v_0 is a depot, while the other vertices represent n clients. A set of permissible visitation times for each client is represented by $H_i = \{S_{i1}, \dots, S_{ih}\}$ and visitor S's visitation schedule outlined by $S = \{l_1, ..., l_T\}$; The customer's demand on day d is indicated by the variable l_d (e.g., $l_d = 0$ shows services to on day d of the customer), and number of days sets are shown in the form of time period T. Following are the notations used [40], [41].

2.1 Notations and variables

- *n* Clients total number
- *m* Vehicles total number
- t Days period
- c_{ij} Travel expense along arc (i, j)
- t_{ij} Travel period along arc (i, j)
- O_i Service period for client *i*
- p_i^d Pick up amount for client *i* in *d* 2 the period of day
- q_i^d Delivery amount of client *i* in *d* 2 the period of the day
- Q_k Capacity of vehicle k
- D_k Time frames for vehicle k to serve all clients
- t_i^{\min} Lower limit of time frames for client *i*
- t_i^{max} Upper limit of time frames for client *i*

© 2022 Little Lion Scientific



| © 2022 Little Lion Scientific | | |
|---|--|---|
| ISSN: 1992-8645 | www.jatit.org E-ISSN: 1 | 817-3195 |
| $\frac{\text{ISSN: 1992-8645}}{a_{dS_i}} = \begin{bmatrix} 1 & \text{if day } d \text{ is in schedule } S_i \\ 0 & \text{otherwise} \end{bmatrix}$ | $v \square a = \square \square \square \square \square \underbrace{ \square}_{k=1}^{m} \underbrace{ \square}_{k=1}^{d} 1 \qquad ; 1 \square i \square n, 1 \square d \square T $ $ \square \square$ | (12) |
| 2.2 Decision variables $v_{is} = \begin{bmatrix} 1 & \text{if schedule } S_i & \text{is selected for client } i \\ 0 & \text{otherwise} \end{bmatrix}$ \mathbb{Z}_{jk}^d Quantity of pick-up orders of client j vehicles | $\begin{array}{c c}n & n+1 \\ \hline & & \mathbb{P} \\ \hline & & & \\ \hline & & & \\ \hline & & & \\ P \\ 1e & & & i = 0 \\ \hline & & & & \\ Ie & & & & \\ \hline & & & & \\ Ie & & & & \\ \hline & & & & \\ \hline & & & & \\ Ie & & & & \\ \hline & & & & \\ \hline & & & & \\ Ie & & & & \\ \hline & & & & \\ Ie & & & & \\ \hline & & & & \\ Ie & & & & \\ \hline & & & & \\ Ie & & & & \\ \hline & & & & \\ Ie & & & & \\ \hline & & & & \\ Ie & & \\ Ie & & \\ Ie & & \\ Ie & $ | (13) |
| k served in d day | $x_{ijk}^{d}, y_{ik}^{d}, v_{is_{i}} \supseteq \{0,1\}; \ \Box(i, j, k, d)$ | (14) |
| \mathbb{Z}_{jk}^{d} Quantity of deliveries orders of client | $j \qquad z_{ijk}^d, \mathbb{P}_{jk}^d, \mathbb{P}_{jk}^d \mathbb{P}\{0,1,2,\ldots\}; \mathbb{P}(i,j,k,d)$ | (15) |
| vehicle k served in d day $\begin{bmatrix} d \\ jk \end{bmatrix}$ Initial service period of client j by vehicle in day d $x_{ik}^{d} = \begin{bmatrix} 11 & \text{if vehicle } k \text{ serve client } j \text{ immediately after client } i \text{ in day } d \\ y_{ik}^{d} = \begin{bmatrix} 1 & \text{if vehicle } k \text{ serve customer } j \text{ in day } d \\ 0 & \text{otherwise} \\ \end{bmatrix}$ $y_{jk}^{d} = \begin{bmatrix} 1 & \text{if vehicle } k \text{ serve customer } j \text{ in day } d \\ 0 & \text{otherwise} \\ \end{bmatrix}$ Vehicle k Load while navigating arc (i, j) is d day 2.3 Mathematical model min $Z = \begin{bmatrix} 2 & 2 & 2 \\ 2 & 2 & 2 & 2 \\ \end{bmatrix}$ $x_{ijk}^{d} = \begin{bmatrix} 2 & 2 & 2 & 2 \\ 2 & 2 & 2 & 2 & 2 \\ \end{bmatrix}$ (1) | (1) and (2) make certain that each vehicle comes at a client's location needs to depart that location as soon as feasible (1), this r that each vehicle allocated to a client must every single day (2). Constraint (3) is design avert capacity of the vehicle from exceeding as webicle k travels the area (i, i). At a minimum | straints ele that rt from equires service gned to ng limit um, the apacity pickup nts (4) system. rvice is as been |
| $\begin{array}{c} \begin{array}{c} \begin{array}{c} \mathbf{z} \\ \mathbf{z} \end{array} \end{array} \right) = \begin{array}{c} \begin{array}{c} \mathbf{z} \\ \mathbf{z} \\ \mathbf{z} \\ \mathbf{z} \\ \mathbf{z} \\ \mathbf{z} \end{array} \\ \mathbf{z} \\ \mathbf{z} \\ \mathbf{z} \\ \mathbf{z} \\ \mathbf{z} \\ \mathbf{z} \end{array} \\ \mathbf{z} \\ \mathbf{z} \\ \mathbf{z} \\ \mathbf{z} \\ \mathbf{z} \end{array} $ | 2) customer within the time limit established node of constraint (8). Constraint (9) conf | ïrms if |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$ | 3) x^d_{ijk} = 1, customer's location j must have an time greater than the total of the custome location S_i arrival times, customer i time of s and arc time of travel (i, j). For each clier one visitation schedule is available constraint 5) For each client, Constraint (11) expresses number of days in their selected schedule, | er's service nt, only nt (10). in the |
| | 6) Will be supplicently franky vertagelies, is the supplicent of t | |

 $\mathbf{P}_{k=1} \stackrel{[]}{\boxtimes} {}^{d} = q^{d}; 1 \stackrel{[]}{\boxtimes} j \stackrel{[]}{\boxtimes} n, 1 \stackrel{[]}{\boxtimes} d \stackrel{[]}{\boxtimes} T$ (6) $\boxed{\begin{smallmatrix} d \\ n+1,k \end{smallmatrix}} \boxed{\begin{smallmatrix} d \\ 2 \end{smallmatrix}} \boxed{\begin{smallmatrix} d \\ ok \end{smallmatrix}} \boxed{\begin{smallmatrix} d \\ 0 \end{smallmatrix}} \boxed{\begin{smallmatrix} d \\ k \end{smallmatrix}} \boxed{\begin{smallmatrix} d \\ k \end{smallmatrix}} \boxed{\begin{smallmatrix} n,1 \end{smallmatrix}} \boxed{\begin{smallmatrix} d \\ 2 \end{smallmatrix}} \boxed{\begin{smallmatrix} d \\ r \end{smallmatrix}} \boxed{\begin{smallmatrix} d \\ r \end{smallmatrix}}$ (7)

$$1 \ j \ i \ n, 1 \ k \ i \ n, 1 \ d \ i \ T \tag{8}$$

$$t_i^{\min}$$
 ?? d_i ? t_i^{\max} ;

$$1 \ 2 \ j \ 2 \ n, 1 \ 2 \ k \ 2 \ m, 1 \ 2 \ d \ 2 \ T \tag{9}$$

$$\mathbb{D}_{ik}^{d} + O_{i} + t \mathbb{D}_{i} \mathbb{D}^{d} \mathbb{D}_{jk} (1\mathbb{D} x^{d}) \mathbb{D}_{jk} M;$$

i 2 *i*, *j* 2 *n*,1 2 *k* 2 *m*,1 2 *d* 2 *T* (10)

within the predetermined timetable. The sub-tour elimination constraint is represented by constraint

the integrality of the variables in the model.

3. THE SOLUTION BASIC APPROACH

Look at an example mixed integer linear programming (MILP) issue that has the succeeding structure.

| | Minimize | $P = c^{\mathrm{T}}x$ | (12) |
|------------|----------|-----------------------|------|
| Subject to | | $Ax \leq b$ | (13) |
| | | $x \ge 0$ | (14) |
| | 2 | | |

 x_j number for approximately $j \in J$ (*J* is index set) (15)

| ISSN: 1992-8645 | www.jatit.org | E-ISSN: 1817-3195 |
|-----------------|---------------|-------------------|
| | | |

the basic feasible vector $(x_B)_k$ component in terms of MILP solution as uninterrupted shown below in equation 16

$$(x_B)_k =$$

 $\mathbb{P}_{k} \mathbb{P}_{k1}(x_{N})_{1} \mathbb{P} \mathbb{P} \mathbb{P}_{kj}(x_{N})_{j} \mathbb{P} \mathbb{P} \mathbb{P}_{k,n\mathbb{Z}m}(x_{N})_{n\mathbb{Z}m} (16)$

This statement can be seen in the Simplex method's final tableau. For example, if $(x_B)_k$ would be an integer variable and we suppose k is not, the fractional and integer elements of k are provided by

$$\mathbb{D}_{k} = \mathbb{D}_{k} \mathbb{I} + f_{k}, \ 0 \mathbb{D} f_{k} \mathbb{D} 1 \tag{17}$$

Supposing bump $(x_B)_k$ up to the closest integer, say $([\beta] + 1)$. We might raise a non-basic variable on the basis of concept of suboptimal elucidations, such as $(x_N)_{j^*}$, exceeding the zero limit, given that α_{kj^*} is a negative component of the vector α_{j^*} . Let Δ_{j^*} be total movement of the non-variable $(x_N)_{j^*}$, and therefore the scalar $(x_B)_k$ numerical value is an integer Δ_{j^*} can then be stated using Eqn. (16) as follows.

$$\mathbb{P}_{f^*} = \frac{1\mathbb{P} f_k}{\mathbb{P} \mathbb{P}_k}$$
(18)

Non-basics remain at a constant 0. As may be observed, by replacing (18) into (16) for $(x_N)_{j^*}$. When we take into consideration (17)'s division of the number *x*, then we get

$$(x_{\rm B})_{\rm k} = [\beta] + 1$$

Therefore, now $(x_B)_k$ becomes an integer.

The importance of a non-basic variable in integerizing the equivalent basic variable has now been established. As a consequence, the following result is required to prove that the integerizing procedure must operate with a non-integer variable. **Theorem.**

If the MILP issue (1)-(4) has an optimum answer, then non-basic variables must be included in the solution. $(x_N)_j$, $j = 1, \Box, n$, should be non-integer

variables. **Proof.**

Using slack variables as a continuous in solving the issue (except in the case of equality constraints, which are non-integer). Assuming x_B is a basic variables of vector including total slack variables, so variables becomes integer values as they are included in the non-basic vector x_N .

As the scalar's $(x_N)_{j^*}$ numerical value increases to Δ_{j^*} , so will the additional components $(x_B)_{i^*k}$ of vector x_B . Thus, if vector α_{j^*} , i.e., α_{j^*} for $i \neq k$, some elements shows positive result. Thus, the x_B element starts decreasing and may potentially reach 0 at some point. Due to the nonnegativity condition, however, vector x no components may becomes less than zero. Because of this, a method named the minimal proportion test is required to determine the non-basic's $(x_N)_{j^*}$ maximum movement while still keeping all of x viable. Two aspects must be included in this ratio test.

Firstly, a basic variable (x_B)_{i*k} reduces to 0 (lower bound).

2. The basic variable, $(x_B)_k$ rises to an integer. If we were to apply these both aspects to each other, we'd do the following:

$$\mathbb{P}_2 = \mathbb{P}_{i^*} \tag{20}$$

Amount of non-basic $(x_N)_{j^*}$ release that allows vector x to remain viable despite its zerobound, depends on the θ^* -ratio test as can be seen below

$$\mathbb{B}^* = \min\left(\mathbb{B}_1, \mathbb{B}_2\right) \tag{21}$$

evidently, if $\mathbb{D} = \mathbb{D}_1$, one of the fundamental variables $(x_B)_{i^*k}$ will reach its lower limit prior to the integer value for $(x_B)_k$. If $\mathbb{D}^* = \mathbb{D}_2$, feasibility is preserved since the fundamental variable $(x_B)_k$ will have an integer value. In the same way, we may decrease the numerical value of the fundamental variable $(x_B)_k$ to its nearest integer $[\beta_k]$. Any positive α_{j^*} -value in this situation corresponds to the movement amount caused by the $(x_N)_{j^*}$ non-basic variable and hence

$$\mathbb{Z}_{f\mathbb{D}} = \frac{f_k}{\mathbb{Z}_{ki}} \tag{22}$$

Ratio test θ^* is still required to keep things feasible. \mathbb{Z} , reflect the particular non basic variable, as represented in equation (18) and (22). The vector α 's corresponding element are the sole factor that researcher must consider during their operations. A vector α_i may be represented as

$$\mathbb{P}_{i} = B^{\mathbb{P}^{1}}a_{i}, \ j = 1, \Box, n \ \mathbb{P} m \tag{23}$$

As a result, to acquire a certain vector \mathbb{Z}_j element one must first identify the associated matrix $[B]^{-1}$ columns. Let's say that we want to find out the α_{kj^*} value allowing v^{T_k} become the *k*-th column vector of $[B]^{-1}$, we will get

$$v_k^T = e_k^T B^{\boxtimes 1} \tag{24}$$

After that, we can calculate α_{kj^*} 's numerical value from

30th June 2022, Vol.100, No 12

© 2022 Little Lion Scientific

| | JULIA |
|-----------------|---------------------|
| wayay istit org | F.ISSN: 1817,3195 |
| www.jactiong | 1. 10014. 101/ 01/0 |
| | |

Eqns. (24) and (25) are stated to as pricing operation in Linear Programming (LP). d_i represents the vector of decreased prices. It is utilized to assess the decrease in the objective function value produced by a non-basic variable releasing from its bounds. When choosing which non-basic to release in the integerization procedure, especial consideration must be taken to the vector $d_{\rm i}$, so that degradation is diminished. A lower limit on any integer-equivalent solution may be found using the minimal continuous solution. The amount of movement in a given non-basic variable as given in Eqn. (18) or (22), is, nevertheless, influenced by the associated α_i -vector element. As a result, releasing a non-basic variable $(x_N)_{i^*}$ results in objective function reduced value. When determining how to integerize *x*, the ratio is:

$$\frac{d_k}{\mathbb{Z}_{kj^*}} \tag{26}$$

Where |a| implies the definite value of scalar a.

To keep the best continuous solution as close to zero as possible, we apply the following technique to determine which non-basic variable raises from its zero limit, that is,

$$\min_{j} \left\| \frac{d_{k}}{d_{k}} \right\|_{k,j^{*}} = 1, \Box, n \ \mathbb{D} m \tag{27}$$

Writing constraints for non-basic (N), basic (B), and superbasic (S), variables may be done using a "active constraint" technique and the splitting of the constraints equivalent to these three variables.

or

$$Bx + Sx + Nx = b$$
(29)

$$x_N = b_N \tag{30}$$

It is supposed that matrix B would be non singular and square matrix but we obtained as follows.

Xs

$$x_B = \mathbb{P} \mathbb{P} W x_S \mathbb{P} \mathbb{P} x_N \tag{31}$$

Where:

$$\boxed{2} = B^{\boxed{2}}b \tag{32}$$

$$W = B^{\mathbb{Z}^1}S \tag{33}$$

$$\mathbb{P} = B^{\mathbb{Z}^1}N \tag{34}$$

Non-basic variables are being kept to their limit in expression (30). Eqn. (31), which uses the integerizing technique mentioned in the preceding section and suited for MILP problems, makes it clear that this strategy may be put into action. A degenerate solution would allow us to liberate a non-basic variable from the constraints of Eqn. (30) and swap it for a basic variable of the same type after integerization.

The basic variable, $(x_B)_k$ is being integerized right now, and as a result, the nonbasic variable, $(c_N)_{j^*}$, is being liberated from its zerobound. Assume that $(x_N)_{j^*}$'s maximum movement fulfills $\mathbb{Z}^* = \mathbb{Z}_{\rightarrow}$.

In order to take use of the method of modifying the basis, $(x_B)_k$ must be integer valued, we transfer $(x_N)_{j^*}$ keen on *B* (to substitute $(x_B)_k$) and integer-valued $(x_B)_k$ into *S* to ensure that the integer solution remains intact. Now that a fundamental variable has reached its limit, we have a degenerate solution. With a fresh set of integers, the process of integerizing continues [*B*, *S*]. As a result, total number of integral variables becomes superbasic.

4. THE ALGORITHM

The following approach may be used to find a suboptimal but integer-feasible solution from an optimum continuous solution once the relaxed issue has been solved. Let

x = [x] + f, 0 2 f 2 1

be the (continuous) solution of the tranquil issue, [x] is the integer component of non-integer variable x and f is the fractional component.

Step 1. Obtaining the smallest integer feasibility of row $i^* = \min\{f_i, 1 \ge f_i\}$

of row
$$l^*$$
, $\mathbb{I}_{i^*} = \min\{J_i, 1\}$

Step 2. Compute
$$v_{i^*}^T = e_{i^*}^T B^{\square 1}$$

this operation is named as pricing operation

Step 3. Compute
$$\mathbb{Z} = v^T a_{i^* j}$$

With *j* match up to $\min_{j \in \mathbb{Z}} \frac{d_j}{|\mathbb{Z}|_{ij}} = I$. For non-basic *j* at lower limit

If
$$\mathbb{D}_{ij} < 0$$
 and $\mathbb{D}_{i^*} = f_i$ determine
(122)
 $\mathbb{D} = \frac{i^*}{\mathbb{D} \mathbb{D}_{ij}}$
If $\mathbb{D} > 0$ and $\mathbb{D} = 1\mathbb{D} f$ determine
(128)

$$\mathbf{D} = \frac{(\mathbf{1} \, \mathbf{D} \, \mathbf{D}_{i^*})}{\mathbf{D}_{ij}}$$

ISSN: 1992-8645

If
$$\mathbb{D}_{ij} < 0$$
 and $\mathbb{D}_{i^*} = 1 \mathbb{D} f_i$ determine

$$\mathbb{D}$$

$$\mathbb{D} = \underbrace{\stackrel{i^*}{\mathbb{D} \mathbb{D}_{ij}}}_{ij}$$
If $\mathbb{D} > 0$ and \mathbb{D}

$$\stackrel{i^*}{=} f_i$$
 determine

$$\mathbb{D} = \underbrace{\frac{\mathbb{D}_{i^*}}{\mathbb{D}_{ij}}}_{ij}$$
II. For non-basic j at upper limit
If $\mathbb{D} < 0$ and $\mathbb{D} = 1\mathbb{D} f$ determine

$$\stackrel{i^*}{=} \underbrace{\mathbb{D} \mathbb{D}_{ij}}_{i^*}$$
If $\mathbb{D} > 0$ and $\mathbb{D} = 1\mathbb{D} f$ determine

$$\mathbb{D} = \underbrace{\frac{(1 \mathbb{D} \mathbb{D}_{i^*})}{\mathbb{D}_{ij}}}_{i^*}$$
If $\mathbb{D} > 0$ and $\mathbb{D} = 1\mathbb{D} f$ determine

$$\mathbb{D} = \underbrace{\frac{(1 \mathbb{D} \mathbb{D}_{i^*})}{\mathbb{D}_{ij}}}_{i^*}$$
If $\mathbb{D} > 0$ and $\mathbb{D} = 1\mathbb{D} f$ determine

$$\mathbb{D} = \underbrace{\mathbb{D}_{i^*}}_{i^*}$$
If $\mathbb{D} < 0$ and $\mathbb{D} = f$ determine

$$\mathbb{D} = \underbrace{\mathbb{D}_{i^*}}_{i^*} = f$$
 determine

$$\mathbb{D} = \underbrace{\mathbb{D}_{i^*}}_{i^*} = f$$
 determine

Else, go to available superbasic j or non integer non basic variable. Finally column j^* is elevated from LB or reduced from UB. If this never happen, then proceed to the next i^* .

Step 4. Compute

$$\begin{split} & \boxed{\mathbb{2}}_{j^*} = B^{\boxed{\mathbb{2}}} \boxed{\mathbb{2}}_{j^*} \\ & \text{i.e., solve } B \boxed{\mathbb{2}}_{j^*} = \boxed{\mathbb{2}}_{j^*} \quad \text{for } \boxed{\mathbb{2}}_{j^*}. \end{split}$$

Step 5. Ratio test: Because non-basic j^* has been released from its limits, there are three possible values for the basic variables.

If j lower limit* Let

$$A = \min_{i^{*}i^{*}|i^{*}|_{i^{*}} > 0} \mathbb{C} \left[\begin{array}{c} x_{B} & \overline{\mathbb{C}} & l_{i^{*}} \\ \hline & & & \\ \vdots^{*}i^{*}|i^{*}|_{i^{*}} > 0} \end{array} \right]$$
$$B = \min_{i^{*}i^{*}|i^{*}|_{i^{*}} < 0} \mathbb{C} \left[\begin{array}{c} & & & \\ & & & \\ \end{array} \right]$$
$$C = \mathbb{C}$$

The j^* maximum movement rely on: $\mathbb{Z}^* = \min(A, B, C)$

Suppose

$$A' = \min_{i \notin i^{\mathbb{D}_{i^*} < 0}} \frac{x_B \mathbb{D} l_{i^*}}{\mathbb{D}_{ij^*}} \mathbb{D}_{ij^*}$$

$$B' = \min_{\substack{i' \equiv i \neq \exists_{ij} \neq 0 \\ \exists i' \equiv i \neq \exists_{ij} \neq 0 \\ \exists i' \equiv i' \equiv i' \equiv 0}} \frac{u_{i'} \boxtimes x_{B_{i'}}}{\boxtimes i'_{j'}} \boxtimes C' = \boxtimes$$

$$C' = \boxtimes$$

The j^* maximum movement rely on:

$$\boxtimes * = \min(A', B', C')$$

- Step 6. Switching basis for all probabilities
 - 1. If A or A'
 - $x_{B_{\mu}}$ befits non-basic at lower limit l_{μ}
 - x_{j^*} befits basic (substitutes $x_{B_{i^*}}$)
 - x_{i*} remains basic non-integer
 - 2. If *B* or *B*'
 - *x*_{B_i} becomes non-basic at upper limit *u*_i.
 - x_{i^*} becomes basic (replaces x_{Bi^*})
 - x_{i^*} remains basic non-integer
 - 3. If *C* or *C*
 - x_{i^*} befits basic (replaces x_{i^*})
 - x_{i^*} becomes super-basic at integervalued

repeat from step 1.

5. COMPUTATIONAL RESULT

EXIT -- OPTIMAL SOLUTION FOUND.

| NO. OF ITERATIONS | 67 |
|-------------------|-------------------|
| OBJECTIVE VALUE | 4.50000000000E+02 |

| NORM OF X | 8.250E+02 | NORM |
|-----------|-----------|------|
| OF PI | 1.735E+02 | |

PROBLEM NAME P OBJECTIVE VALUE 4.500000000E+02

STATUS OPTIMAL SOLN

ITERATION 67

1

Table 1: The values of variable

| 1 | X011 | 0.00000 |
|---|------|---------|
| 2 | X021 | 0.00000 |
| 3 | X031 | 0.00000 |
| 4 | X041 | 1.00000 |
| 5 | X012 | 0.00000 |
| 6 | X022 | 0.00000 |
| 7 | X032 | 1.00000 |
| 8 | X042 | 0.00000 |
| 9 | X101 | 1.00000 |

Journal of Theoretical and Applied Information Technology

30th June 2022. Vol.100. No 12 © 2022 Little Lion Scientific

ISSN: 1992-8645

www.jatit.org



| 10 | X201 | 0.00000 |
|----|------------|-------------|
| 11 | X301 | 0.00000 |
| 12 | X401 | 0.00000 |
| 13 | X102 | 1.00000 |
| 14 | X202 | 0.00000 |
| 15 | X302 | 0.00000 |
| 16 | X402 | 0.00000 |
| 17 | X121 | 1.00000 |
| 18 | X131 | 0.00000 |
| 19 | X141 | 0.00000 |
| 20 | X122 | 0.00000 |
| 21 | X132 | 0.00000 |
| 22 | X142 | 0.00000 |
| 23 | X211 | 1.00000 |
| 24 | X231 | 0.00000 |
| 25 | X241 | 0.00000 |
| 26 | X212 | 0.00000 |
| 27 | X232 | 0.00000 |
| 28 | X242 | 0.00000 |
| 29 | X311 | 0.00000 |
| 30 | X321 | 0.00000 |
| 31 | X341 | 0.00000 |
| 32 | X312 | 1.00000 |
| 33 | X322 | 0.00000 |
| 34 | X342 | 0.00000 |
| 35 | X411 | 1.00000 |
| 36 | X421 | 0.00000 |
| 37 | X431 | 0.00000 |
| 38 | X412 | 0.00000 |
| 39 | X422 | 0.00000 |
| 40 | X432 | 0.00000 |
| 41 | L11 | 0.00000 |
| 42 | L21 | 325.00000 |
| 43 | L21 L31 | 825.00000 |
| 44 | L31 L41 | 0.00000 |
| 45 | L11 L12 | 825.00000 |
| 45 | L12 L22 | 0.00000 |
| 40 | L22 L32 | 825.00000 |
| - | L32 L42 | 0.00000 |
| 48 | 1.44.7 | () () () () |

6. CONCLUSION

The prior models failed to consider the true complexity of many real-world routing issues. To suit a variety of practical needs, we've developed a PVRP, or periodic vehicle routing problem in this research, incorporating the PVRP's well-known models. Furthermore, it incorporates plenty of formerly unconsidered upgrades from prior models. This paper has presented a split service of CPVRP that includes the ability to divide a customer's transportation needs across several vehicles. In a transportation system, this issue might arise when a large number of vehicles must pass through a node or client. Another possibility is that the order in certain nodes exceeds the fleet's total capacity. For the purpose of this research, we have sought to optimize the fleet's capacity utilization. As a result, numerous vehicles might meet the needs of certain clients. The provided approach is capable of finding the most costeffective routes for a fleet. It is clear that the suggested PVRP model can be solved using the PSO method, as shown by the simulation results. parameters The PSO and programming implementation may be improved, though, since it was not the greatest. A better solution and a shorter calculation time are now possible thanks to these additional efforts. Additional studies should be done to expand the approach to more complex realworld issues.

REFERENCES:

- N. Christofides, A. Mingozzi, and P. Toth, "The Vehicle Routing Problem," in *Combinatorial Optimization*, N. Christofides, A. Mingozzi, P. Toth, and C. Sandi, Eds. Wiley, 1978, pp. 315–338.
- [2] P. Toth and D. Vigo, *The vehicle routing problem*. SIAM, 2002.
- [3] M. Ostermeier, T. Henke, A. Hübner, and G. Wäscher, "Multi-compartment vehicle routing problems: State-of-the-art, modeling framework and future directions," *Eur. J. Oper. Res.*, vol. 292, no. 3, pp. 799– 817, 2021.
- [4] H. Li, J. Chen, F. Wang, and M. Bai, "Ground-vehicle and unmanned-aerialvehicle routing problems from two-echelon scheme perspective: A review," *Eur. J. Oper. Res.*, vol. 294, no. 3, pp. 1078–1095, 2021.
- [5] G. Laporte and F. Semet, "Classical Heuristics for the Capacitated VRP," in *The Vehicle Routing Problem*, P. Toth and D. Vigo, Eds. SIAM, 2002, pp. 109–128.
- [6] J.-F. Cordeau, G. Desaulniers, J. Desrosiers, M. M. Solomon, and F. Soumis, "The VRP with Time Windows," in *The Vehicle Routing Problem*, P. Toth and D. Vigo, Eds. Philadelpia, Pa: SIAM Monographs on Discrete Mathematics and Applications, 2002, pp. 157–193.
- [7] N. Norouzi, R. Tavakkoli-Moghaddam, M. Ghazanfari, M. Alinaghian, and A. Salamatbakhsh, "A new multi-objective

www.jatit.org



competitive open vehicle routing problem solved by particle swarm optimization," *Networks Spat. Econ.*, vol. 12, no. 4, pp. 609–633, 2012.

[8] M. Savelsbergh and M. Sol, "Drive: Dynamic routing of independent vehicles," *Oper. Res.*, vol. 46, no. 4, pp. 474–490, 1998.

ISSN: 1992-8645

- [9] M. W. P. Savelsbergh and M. Sol, "The general pickup and delivery problem," *Transp. Sci.*, vol. 29, no. 1, pp. 17–29, 1995.
- [10] G. Hasle, "Heuristics for rich VRP models," in *Seminar at GERAD*, 2003, vol. 30, p. 2003.
- [11] H. N. Psaraftis, "Dynamic vehicle routing: Status and prospects," *Ann. Oper. Res.*, vol. 61, no. 1, pp. 143–164, 1995.
- [12] H. N. Psaraftis, "Dynamic vehicle routing problems," *Veh. routing Methods Stud.*, vol. 16, pp. 223–248, 1988.
- [13] R. Tavakkoli-Moghaddam, N. Safaei, M. M. O. Kah, and M. Rabbani, "A new capacitated vehicle routing problem with split service for minimizing fleet cost by simulated annealing," *J. Franklin Inst.*, vol. 344, no. 5, pp. 406–425, 2007.
- [14] B. Eksioglu, A. V. Vural, and A. Reisman, "The vehicle routing problem: A taxonomic review," *Comput. Ind. Eng.*, vol. 57, no. 4, pp. 1472–1483, Nov. 2009.
- [15] R. Russell and W. Igo, "An assignment routing problem," *Networks*, vol. 9, no. 1, pp. 1–17, 1979.
- [16] N. Christofides and J. E. Beasley, "The period routing problem," *Networks*, vol. 14, no. 2, pp. 237–256, 1984.
- [17] M. W. Carter, J. M. Farvolden, G. Laporte, and J. Xu, "Solving an integrated logistics problem arising in grocery distribution," *INFOR Inf. Syst. Oper. Res.*, vol. 34, no. 4, pp. 290–306, 1996.
- [18] J. Alegre, M. Laguna, and J. Pacheco, "Optimizing the periodic pick-up of raw materials for a manufacturer of auto parts," *Eur. J. Oper. Res.*, vol. 179, no. 3, pp. 736– 746, 2007.
- [19] E. J. Beltrami and L. D. Bodin, "Networks and vehicle routing for municipal waste collection," *Networks*, vol. 4, no. 1, pp. 65– 94, 1974.
- [20] A. Rusdiansyah and D. Tsao, "An integrated model of the periodic delivery

problems for vending-machine supply chains," *J. Food Eng.*, vol. 70, no. 3, pp. 421–434, 2005.

- [21] E. Hadjiconstantinou and R. Baldacci, "A multi-depot period vehicle routing problem arising in the utilities sector," *J. Oper. Res. Soc.*, vol. 49, no. 12, pp. 1239–1248, 1998.
- [22] R. Liu, X. Xie, and T. Garaix, "Hybridization of tabu search with feasible and infeasible local searches for periodic home health care logistics," *Omega*, vol. 47, pp. 17–32, 2014.
- [23] E. A. Silver, "An overview of heuristic solution methods," J. Oper. Res. Soc., vol. 55, no. 9, pp. 936–956, 2004.
- [24] S. Pirkwieser and G. R. Raidl, "A variable neighborhood search for the periodic vehicle routing problem with time windows," in *Proceedings of the 9th EU/meeting on metaheuristics for logistics and vehicle routing, Troyes, France*, 2008, pp. 23–24.
- [25] V. C. Hemmelmayr, K. F. Doerner, and R. F. Hartl, "A variable neighborhood search heuristic for periodic routing problems," *Eur. J. Oper. Res.*, vol. 195, no. 3, pp. 791– 802, 2009.
- [26] R. T. Moghaddam, A. M. Zohrevand, and K. Rafiee, "Solving a New Mathematical Model for a Periodic Vehicle Routing Problem by Particle Swarm Optimization," *Transp. Res. J.*, vol. 2, no. 1, pp. 77–87, 2012.
- [27] P. K. Nguyen, T. G. Crainic, and M. Toulouse, "A hybrid generational genetic algorithm for the periodic vehicle routing problem with time windows," *J. Heuristics*, vol. 20, no. 4, pp. 383–416, 2014.
- [28] L. Trihardani and O. A. C. Dewi, "Pengembangan Algoritma Hybrid Metaheuristik Untuk Penentuan Rute Pengiriman Produk Perishable," J. Tek. Ind., vol. 18, no. 2, pp. 191–206, 2017.
- [29] D. Aksen, O. Kaya, F. S. Salman, and Ö. Tüncel, "An adaptive large neighborhood search algorithm for a selective and periodic inventory routing problem," *Eur. J. Oper. Res.*, vol. 239, no. 2, pp. 413–426, 2014.
- [30] P. M. Francis, K. R. Smilowitz, and M. Tzur, "The period vehicle routing problem and its extensions," in *The vehicle routing problem: latest advances and new challenges*, Springer, 2008, pp. 73–102.

| | © 2022 Little Lion Scientific | TITAL |
|---------|---|-------------------|
| ISSN: | 1992-8645 <u>www.jatit.org</u> | E-ISSN: 1817-3195 |
| [31] | T. Vidal, T. G. Crainic, M. Gendreau, N. Lahrichi, and W. Rei, "A hybrid genetic algorithm for multidepot and periodic vehicle routing problems," <i>Oper. Res.</i> , vol. 60, no. 3, pp. 611–624, 2012. | |
| [32] | C. Archetti, E. Fernández, and D. L.Huerta- Muñoz, "The flexible periodic vehicle routing problem," <i>Comput. Oper. Res.</i> , vol. 85, pp. 58–70, 2017. | |
| [33] | R. Liu, X. Xie, V. Augusto, and C. Rodriguez, "Heuristic algorithms for a vehicle routing problem with simultaneous delivery and pickup and time windows in home health care," <i>Eur. J. Oper. Res.</i> , vol. 230, no. 3, pp. 475–486, 2013. | |
| [34] | D. Mathelinea, R. Chandrashekar, and N. F. A. C. Omar, "Inventory cost optimization through nonlinear programming with constraint and forecasting techniques," in <i>AIP Conference Proceedings</i> , 2019, vol. 2184. | |
| [35] | P. Francis, K. Smilowitz, and M. Tzur, "The period vehicle routing problem with service choice," <i>Transp. Sci.</i> , vol. 40, no. 4, pp. 439–454, 2006. | |
| [36] | AK. Rothenbächer, "Branch-and-price- and-cut for the periodic vehicle routing problem with flexible schedule structures," <i>Transp. Sci.</i> , vol. 53, no. 3, pp. 850–866, 2019. | |
| [37] | C. Archetti, E. Fernández, and D. L.Huerta- Muñoz, "A two-phase solutionalgorithm for the Flexible Periodic Vehicle Routing Problem," <i>Comput. Oper. Res.</i> , vol. 99, pp. 27–37, 2018. | |
| [38] | M. Darvish, C. Archetti, L. C. Coelho, and M. G. Speranza, "Flexible two-echelon location routing problem," <i>Eur. J. Oper.</i> <i>Res.</i> , vol. 277, no. 3, pp. 1124–1136, 2019. | |
| 39] | A. Estrada-Moreno, M. Savelsbergh, A. A. Juan, and J. Panadero, "Biased-randomized iterated local search for a multiperiod vehicle routing problem with price discounts for delivery flexibility," <i>Int. Trans. Oper. Res.</i> , vol. 26, no. 4, pp. 1293–1314, 2019. | |
| [40] | E. Angelelli and M. G. Speranza, "The periodic vehicle routing problem with intermediate facilities," <i>Eur. J. Oper. Res.</i> , vol. 137, no. 2, pp. 233–247, 2002. | |
| F / 1] | | |

A. Goel and V. Gruhn, "A general vehicle [41] routing problem," Eur. J. Oper. Res., vol. 191, no. 3, pp. 650–660, 2008.

jurnal 11 vol100

ORIGINALITY REPORT



Submitted to Universitas International Batam Student Paper

